On the spectrum of Schrödinger-type operators: the case of potentials with local singularities

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April 10, 2021

Abstract

The goal of this talk is twofold. We prove that the operator H = L+V, the perturbation of the Taibleson-Vladimirov multiplier $L = \mathfrak{D}^{\alpha}$ by the potential $V(x) = b ||x||^{-\alpha}$, $b \ge b_*$, is essentially self-adjoint and non-negative definite (the critical value b_* depends on α and will be specified in our talk). While the operator H is non-negative definite the potential V(x) may well take negative values, e.g. $b_* < 0$ for all $0 < \alpha < 1$. The equation Hu = v admits a Green function $G_H(x, y)$, the integral kernel of the operator H^{-1} . We obtain sharp lower- and upper bounds on the ratio of the functions $G_H(x, y)$ and $G_L(x, y)$. Examples illustrate our exposition.